

My Lectures from : Purcell Chapter 9

Web Notes : Lecture Notes #8 and #9

Other Notes: EM_Waves

Purcell Problems:

- 9.01 What is magnetic field?
- 9.02 rms magnetic field strength
- 9.03 Where is the proton - electric field only?
- 9.04 Where is the proton - magnetic field also?
- 9.05 Satisfy Maxwell's equations 1
- 9.06 Satisfy Maxwell's equations 2
- 9.07 Plane EM wave

1. A spherical wave - Let the electric field be given by

$$\vec{E}(r, \theta, \phi, t) = A \frac{\sin \theta}{r} \left[\cos(kr - \omega t) - \frac{1}{kr} \sin(kr - \omega t) \right] \hat{\phi}$$

where $\omega/k = c$.

- (a) Show that \vec{E} obeys all four of Maxwell's equations in vacuum, and find the associated magnetic field.
- (b) Calculate the Poynting vector. Average \vec{S} over a full cycle to get the intensity vector \vec{I} .
- (c) Integrate $\vec{I} \cdot d\vec{a}$ over a spherical surface to determine the total power radiated.

2. Discovery of magnetic charge - This problem will explore some of the similarities between electric and magnetic fields. Let us say that magnetic charge has been discovered, called magnetic monopoles. We will work in a system where the units of magnetic charge density μ are chosen so that $\nabla \cdot \vec{B} = 4\pi\mu$.

- (a) When the monopole is in motion, there is a magnetic current density $\vec{L} = \mu\vec{v}$ analogous to the electric current density. Write down the continuity equation for magnetic charge in differential form.
- (b) Write down the new Maxwell's equations in differential form, including the effects of these monopoles.

3. Pair of electric and magnetic fields - A pair of electric and magnetic fields are given by:

$$\vec{E} = E_0 \cos(\alpha y - \gamma z + \delta t) \hat{x}$$

and

$$\vec{B} = B_0 \cos(\alpha y - \gamma z + \delta t) (\hat{y} + \hat{z})$$

By substituting into Maxwell's equations in vacuum, derive the conditions that the constants α , γ , δ , E_0 , and B_0 must obey to satisfy them. Is this a legitimate electromagnetic wave? Why?